



UNIVERSITY OF LISBON
INTERDISCIPLINARY STUDIES
ON SUSTAINABLE ENVIRONMENT AND SEAS



ulisses.ulisboa.pt



University Network for Innovation,
Technology and Engineering

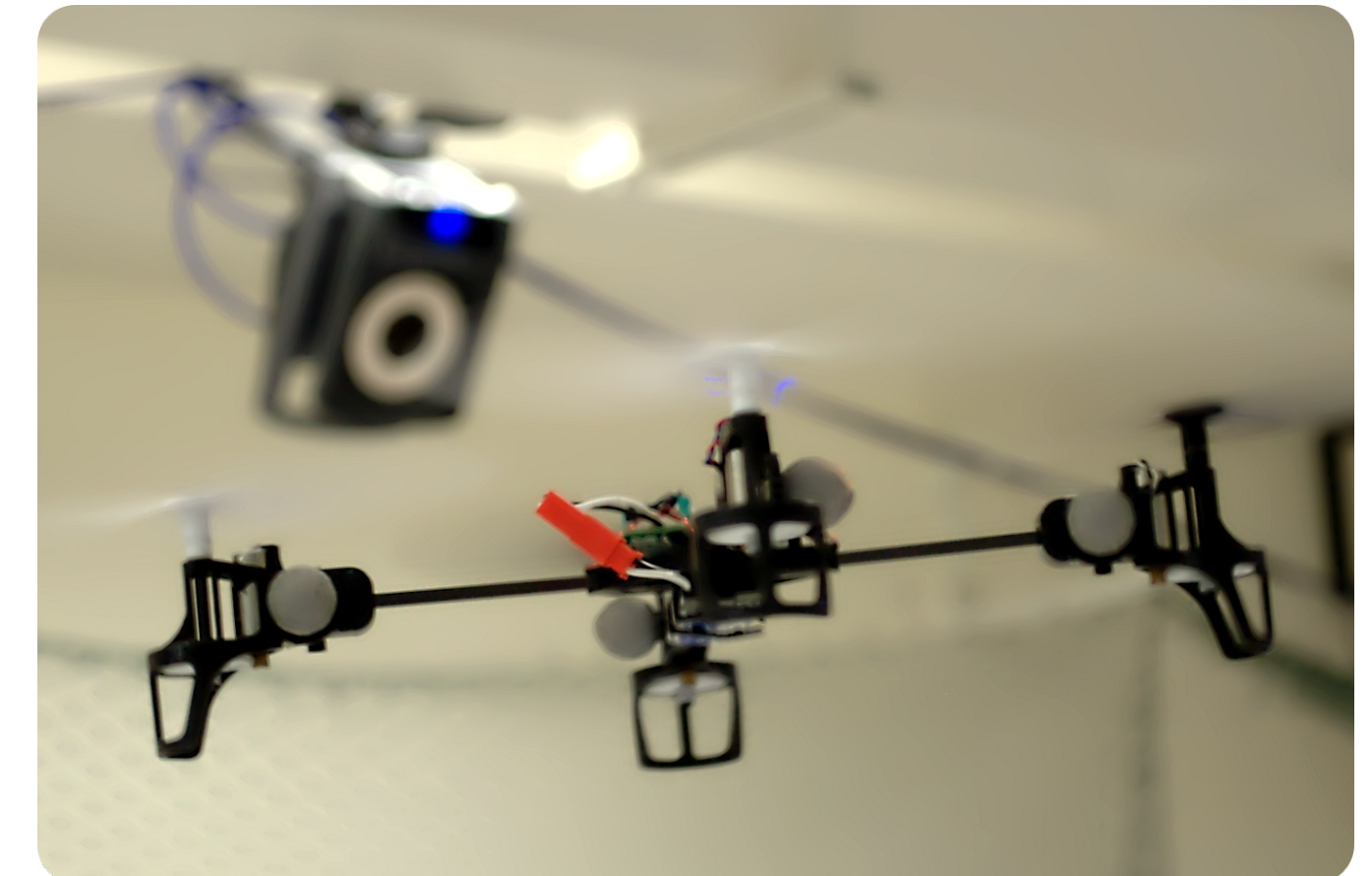


UNIVERSIDADE
DE LISBOA



Aerial Vehicles for missions at sea

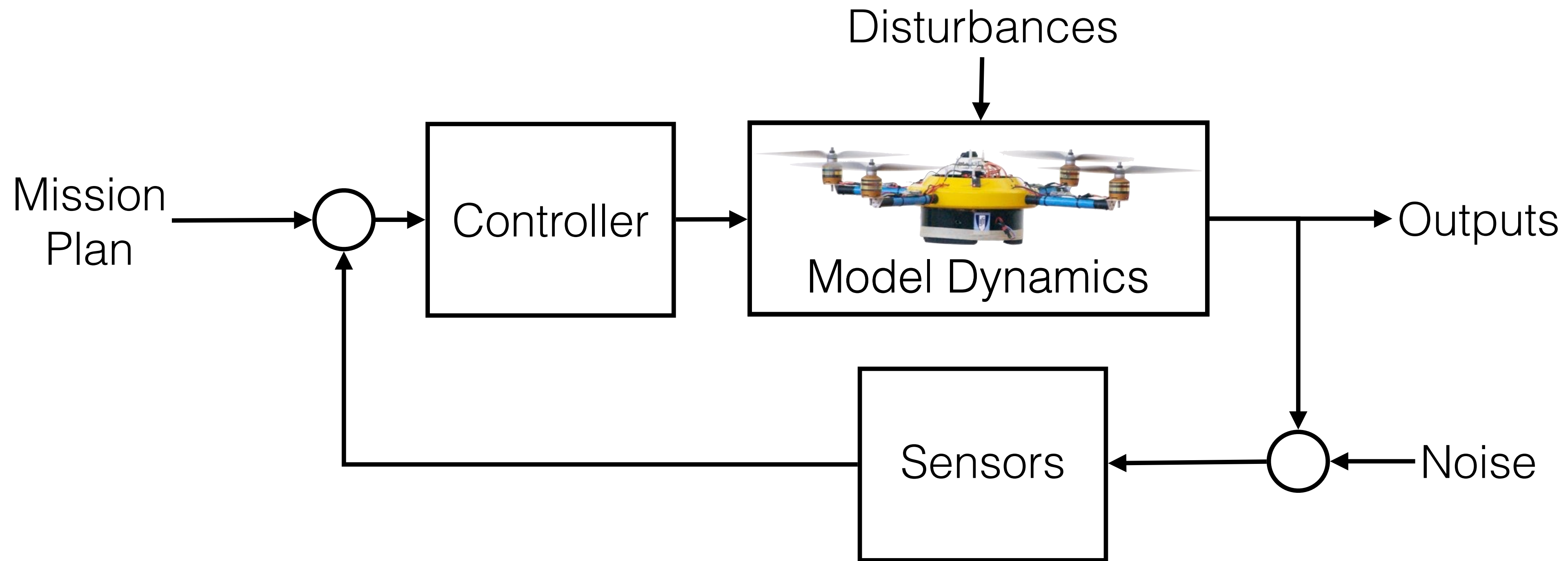
(Part II)



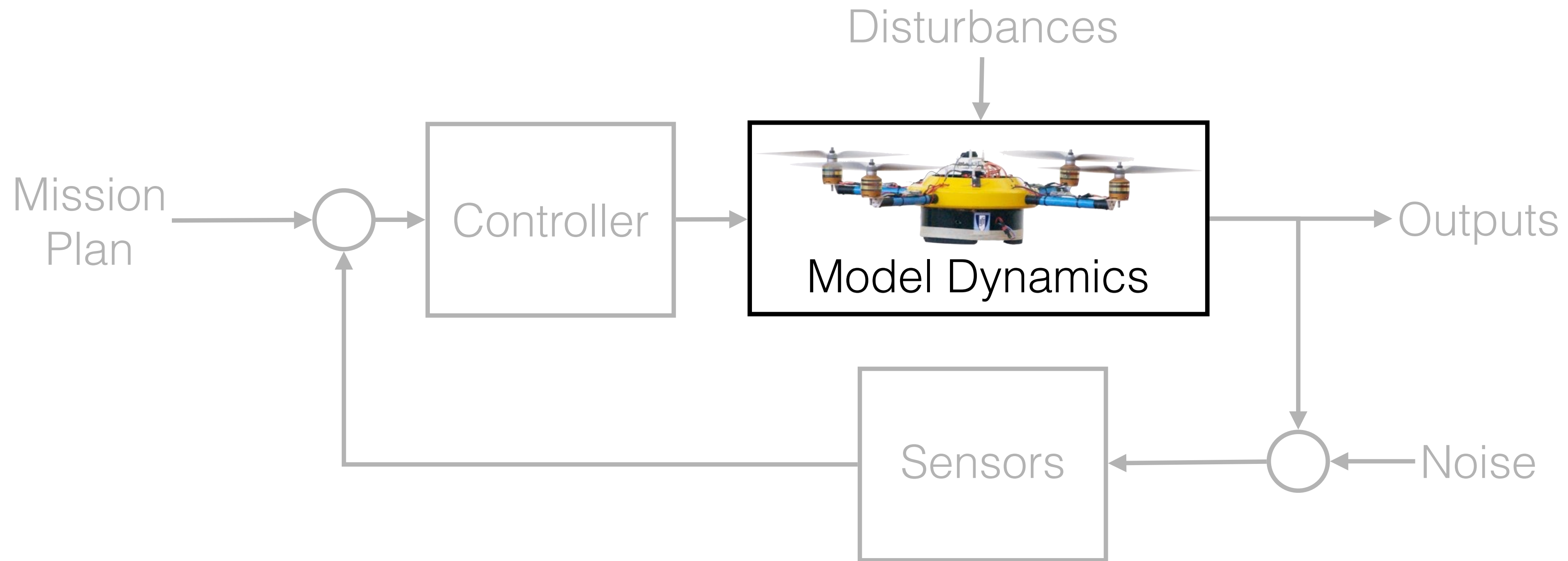
Rita Cunha

Lisboa, May 2020

The quadrotor as a control system



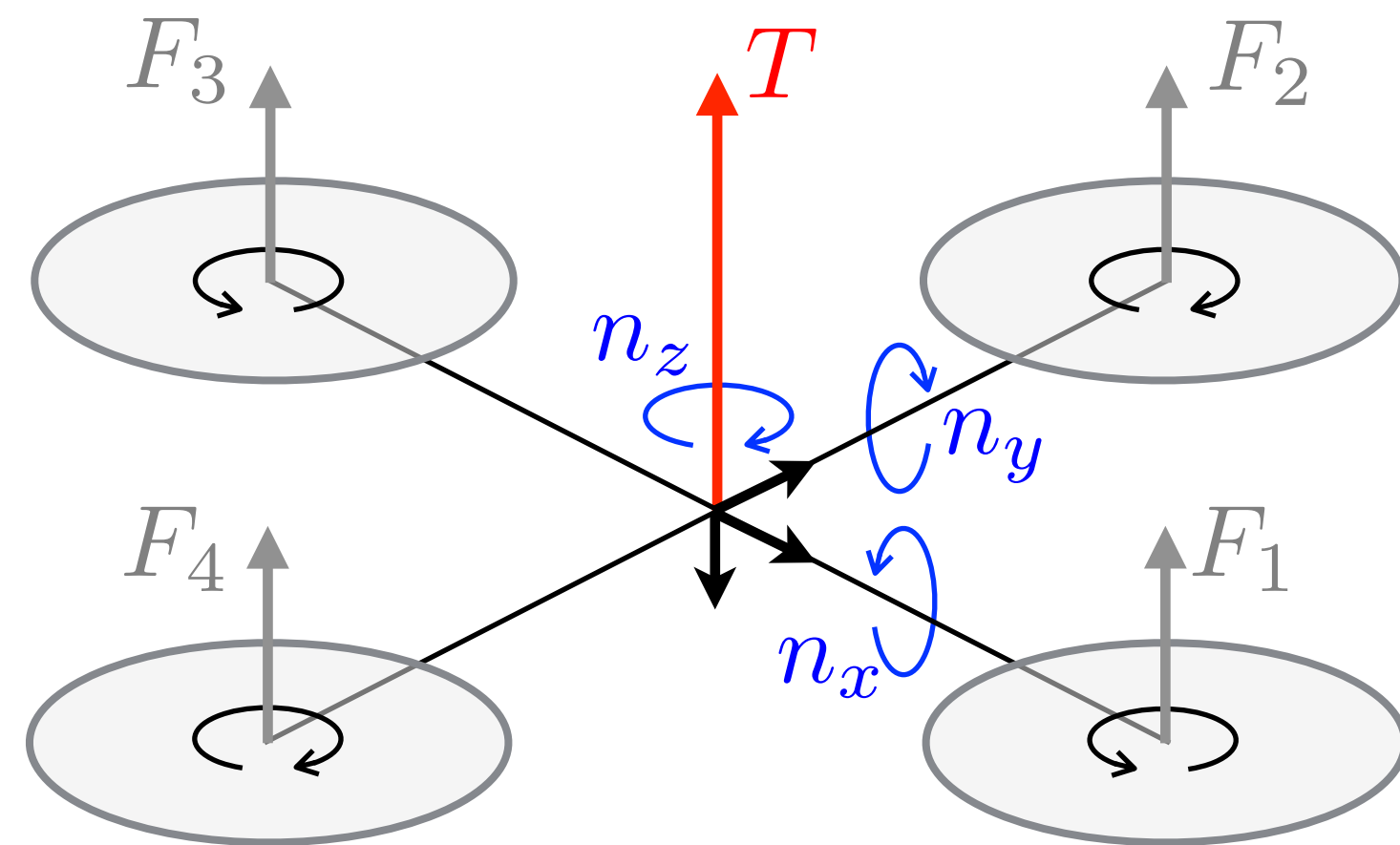
The quadrotor as a control system



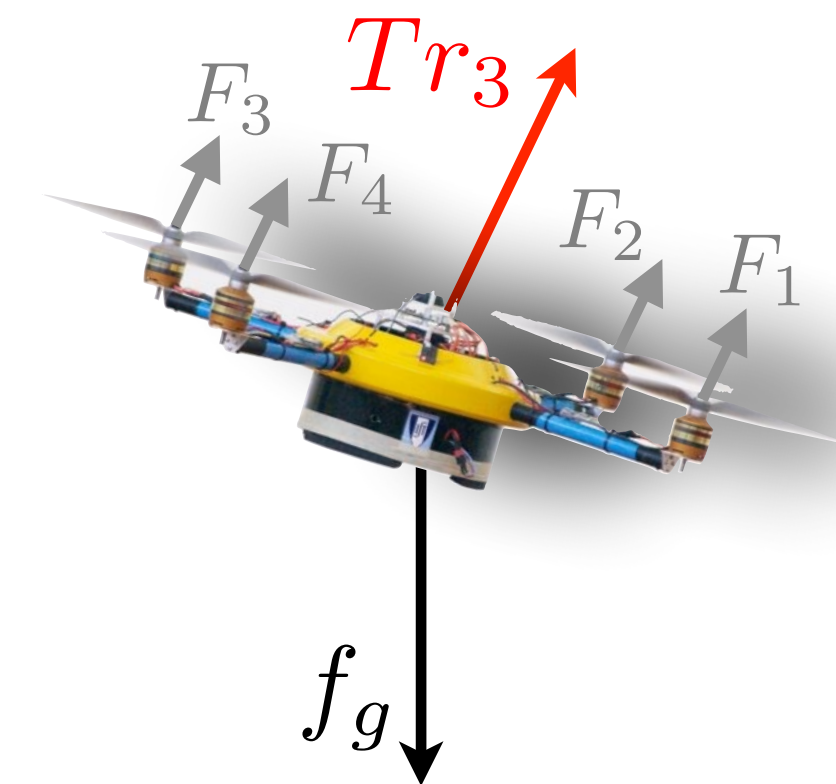
Let's start with the model

Quadrotor forces and moments

Two pairs of counter-rotating rotors



$$\begin{bmatrix} T \\ n_x \\ n_y \\ n_z \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & b & 0 & -b \\ -b & 0 & b & 0 \\ c & -c & c & -c \end{bmatrix} \begin{bmatrix} F_1 \\ F_2 \\ F_3 \\ F_4 \end{bmatrix}$$



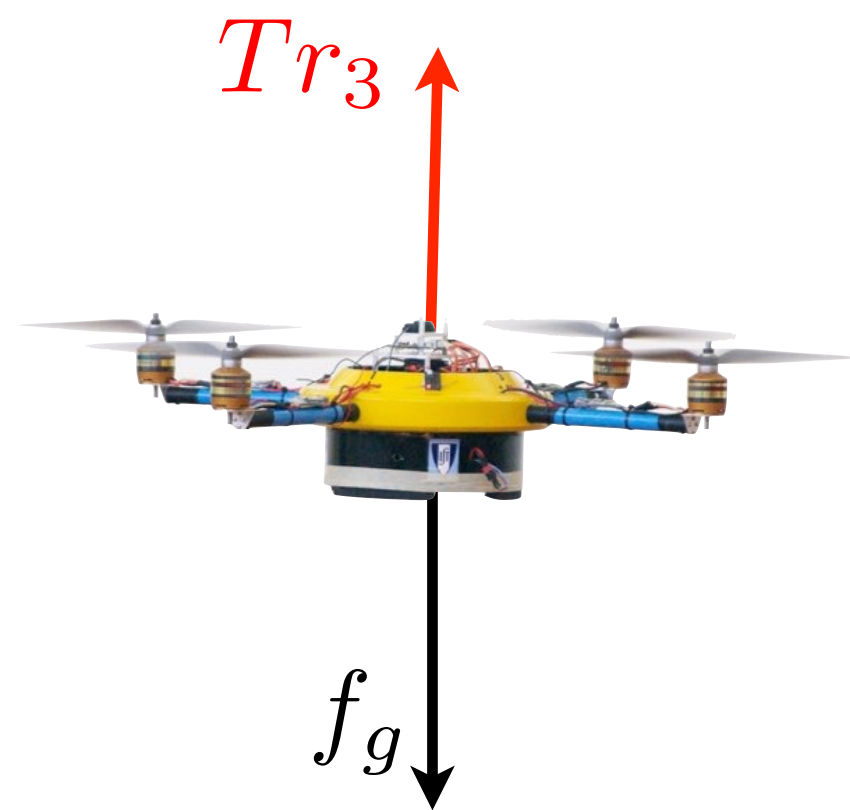
$$r_3 = Re_3 = R \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$f_g = mge_3$$

Quadrotor forces

Underactuated system: 12 states, 4 inputs

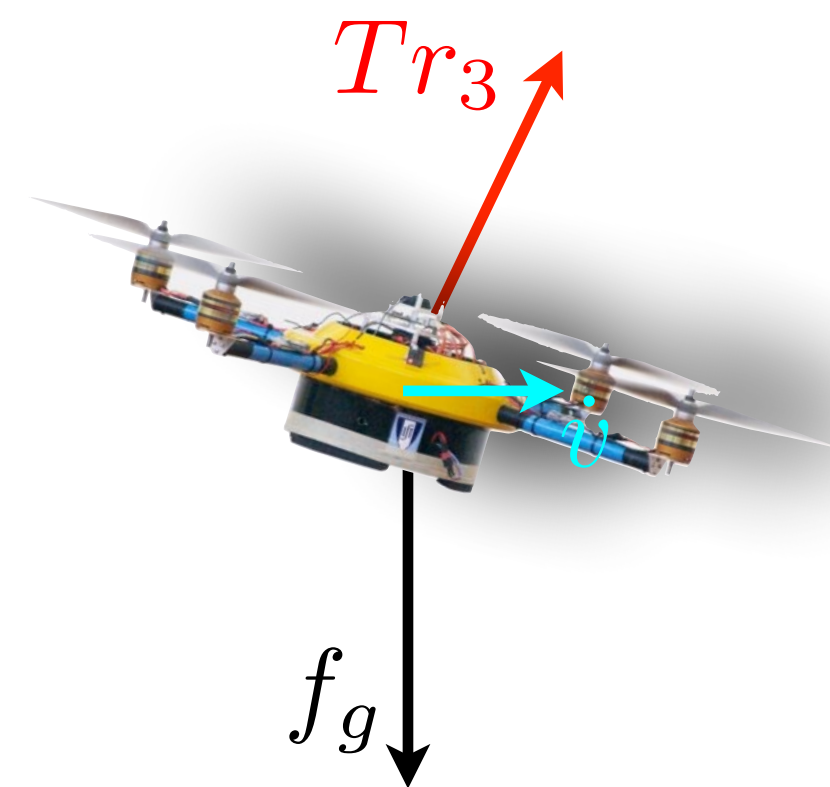
At rest



$$v = 0$$

$$Tr_3 = f_g$$

Accelerating



$$\dot{v} \neq 0$$

$$Tr_3 = f_g - m\dot{v}$$

Control objective:

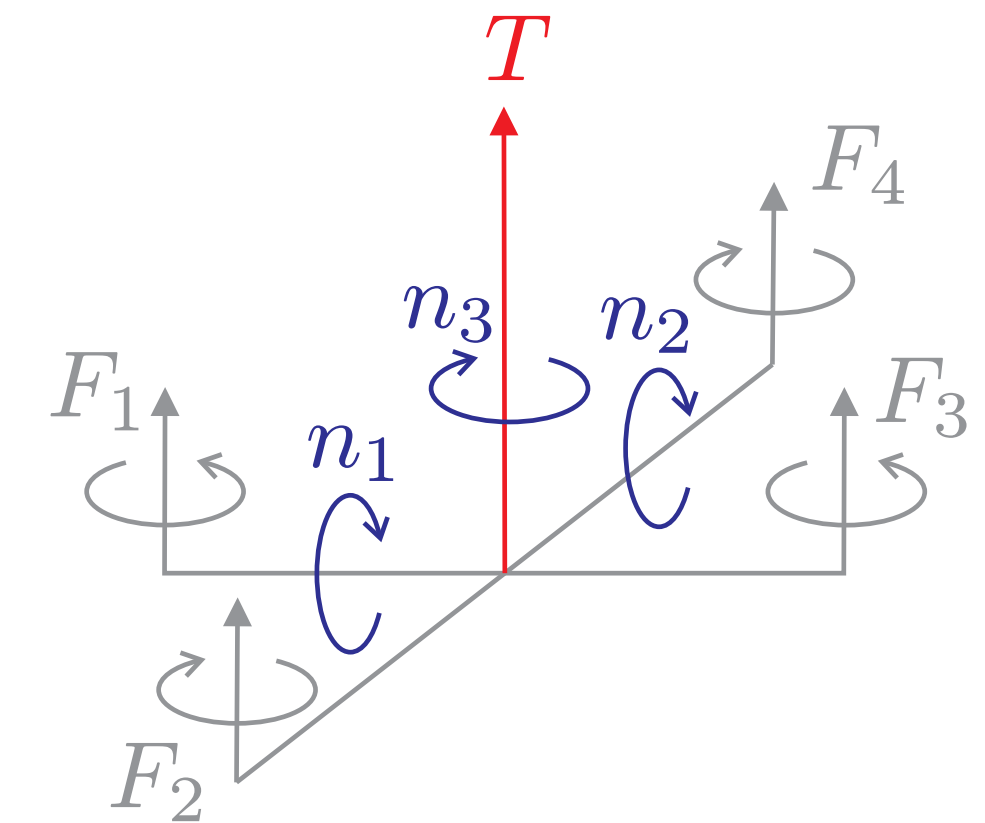
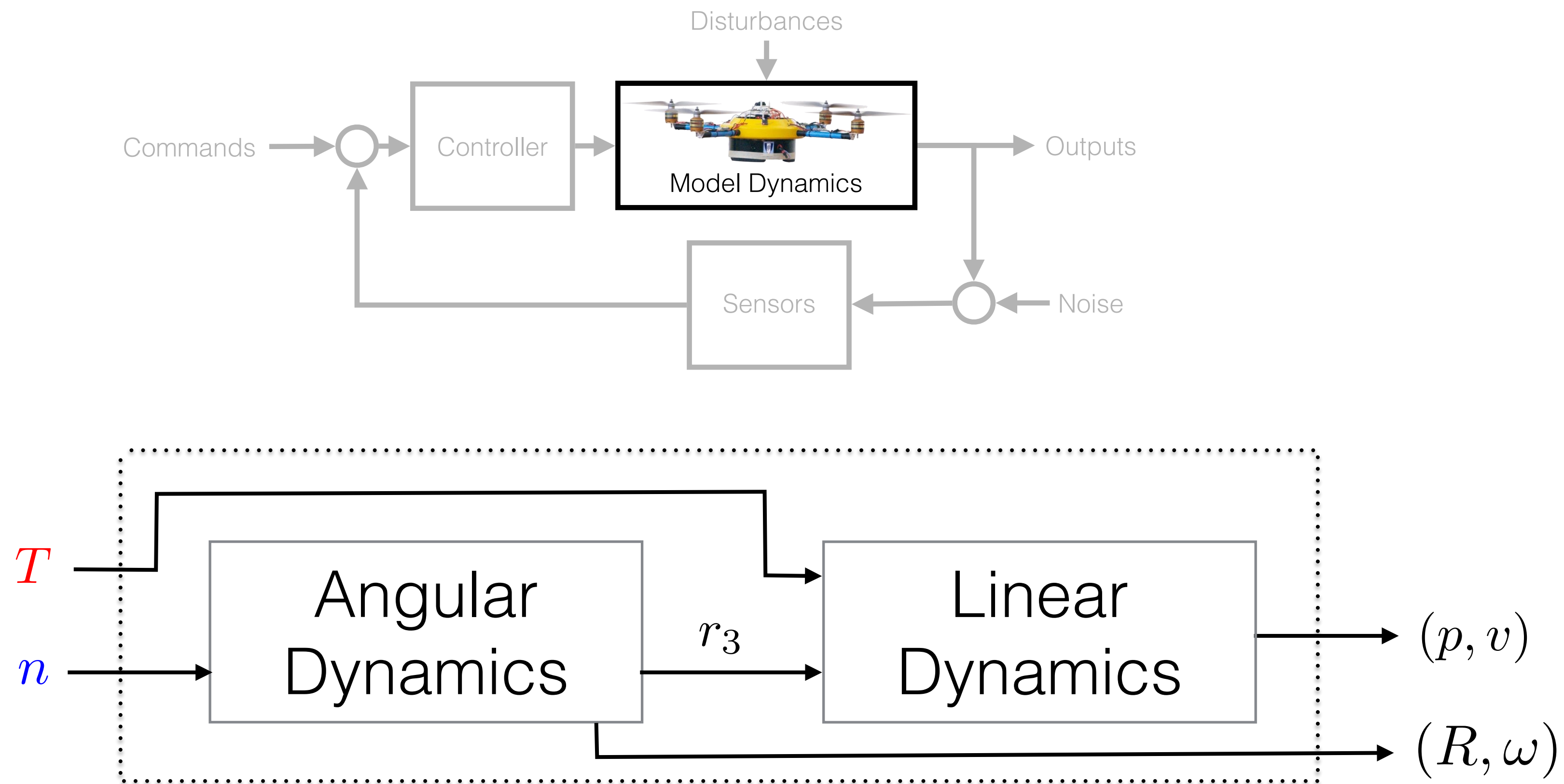
Steer the position to a desired trajectory

$$p(t) \rightarrow p_d(t)$$

using (T, n) as inputs.

Can only prescribe 4 states:
3D position and rotation about z-axis

Quadrotor dynamic model

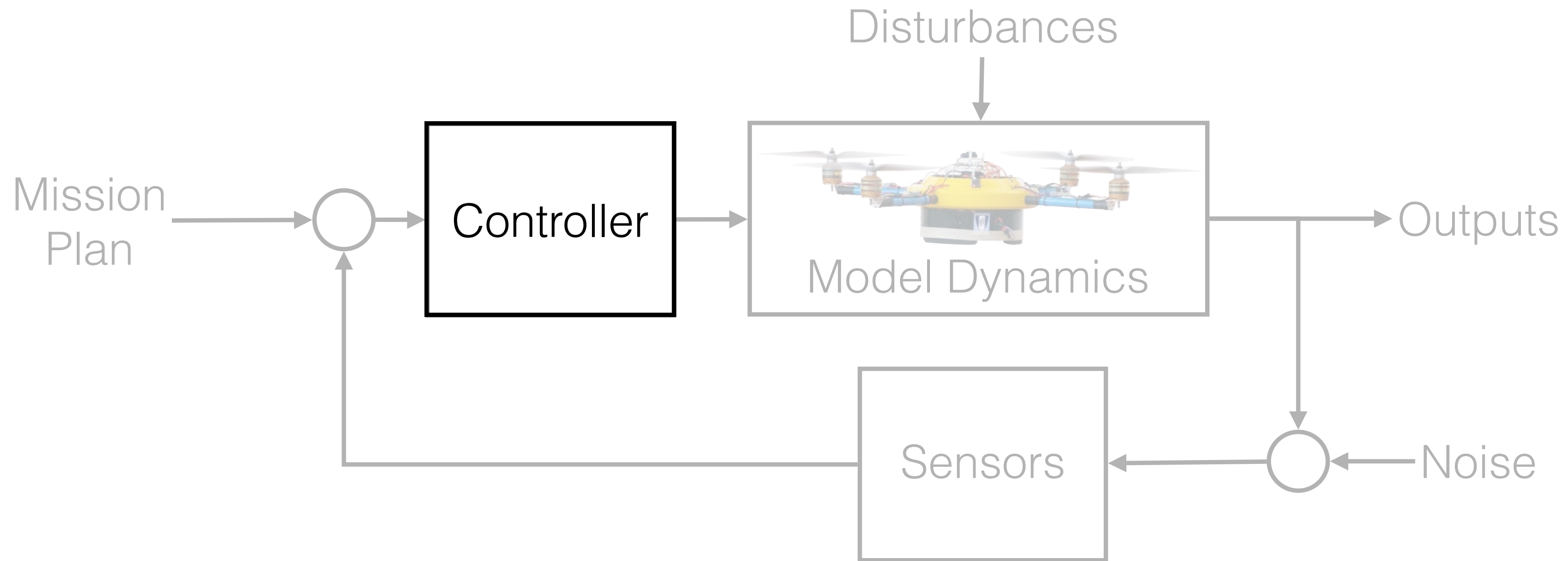


State (p, v, R, ω)

Input (T, n)

Can prescribe $(p, \psi) \in \mathbb{R}^4$

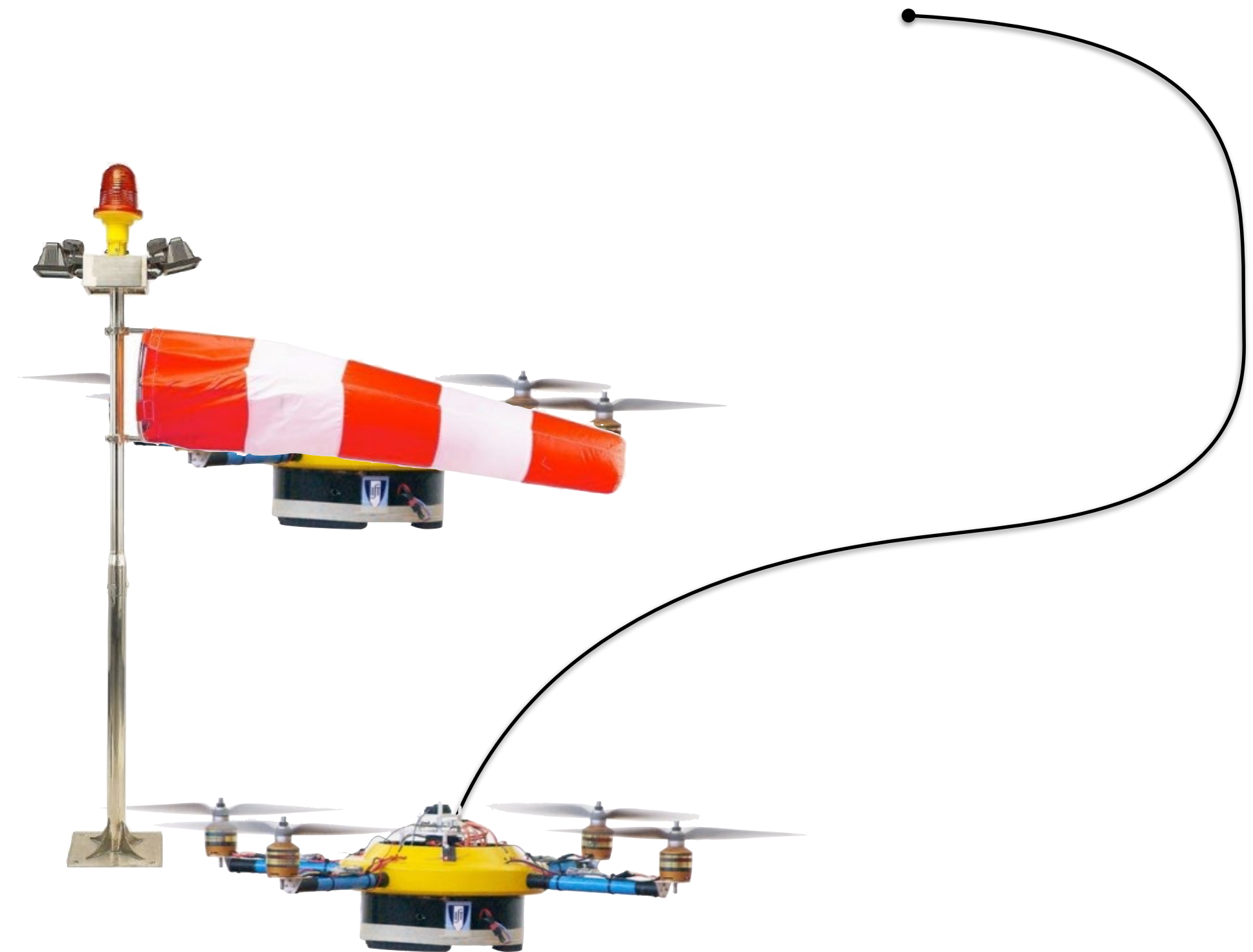
The quadrotor as a control system



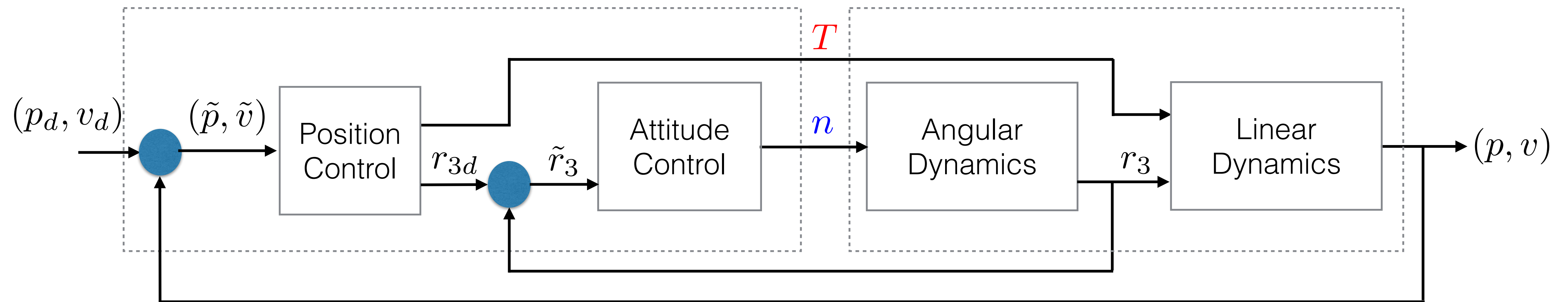
Now the controller

Trajectory Tracking - Control Objectives

- Track a trajectory
- Realistic model
- Robustness to disturbances
- Actuation bounds
- Large basin of attraction



Trajectory Tracking Control

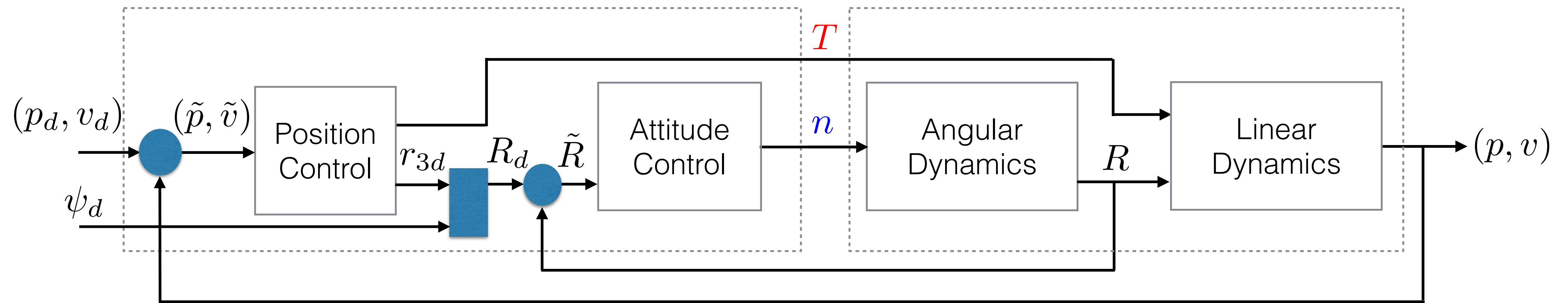


*Simplest Position Controller
yields a mass-spring-damper
system*

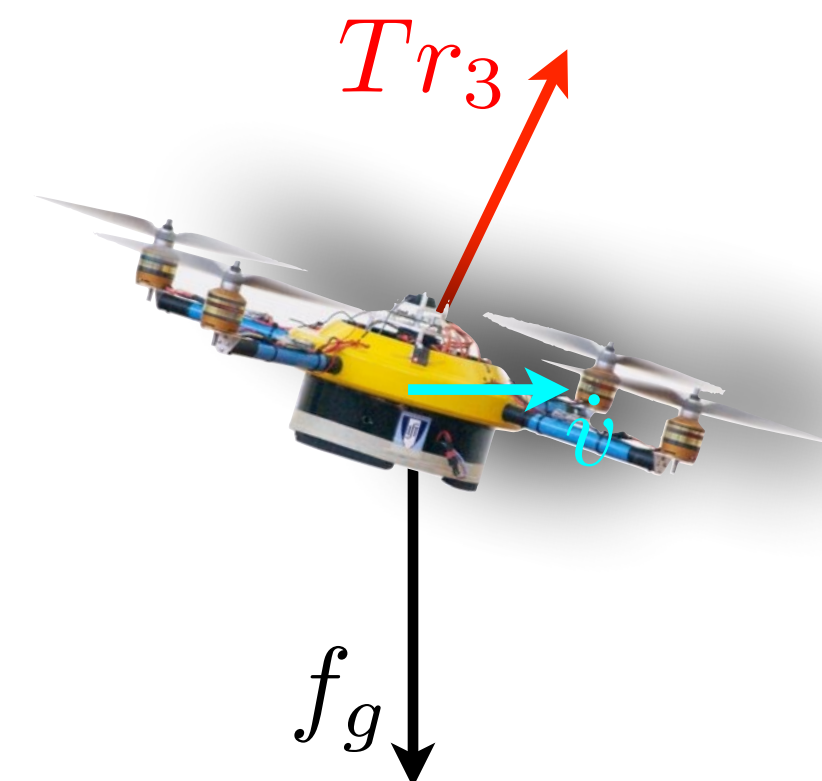
$$m\ddot{\tilde{v}} = -k_1\tilde{p} - k_2\tilde{v}$$



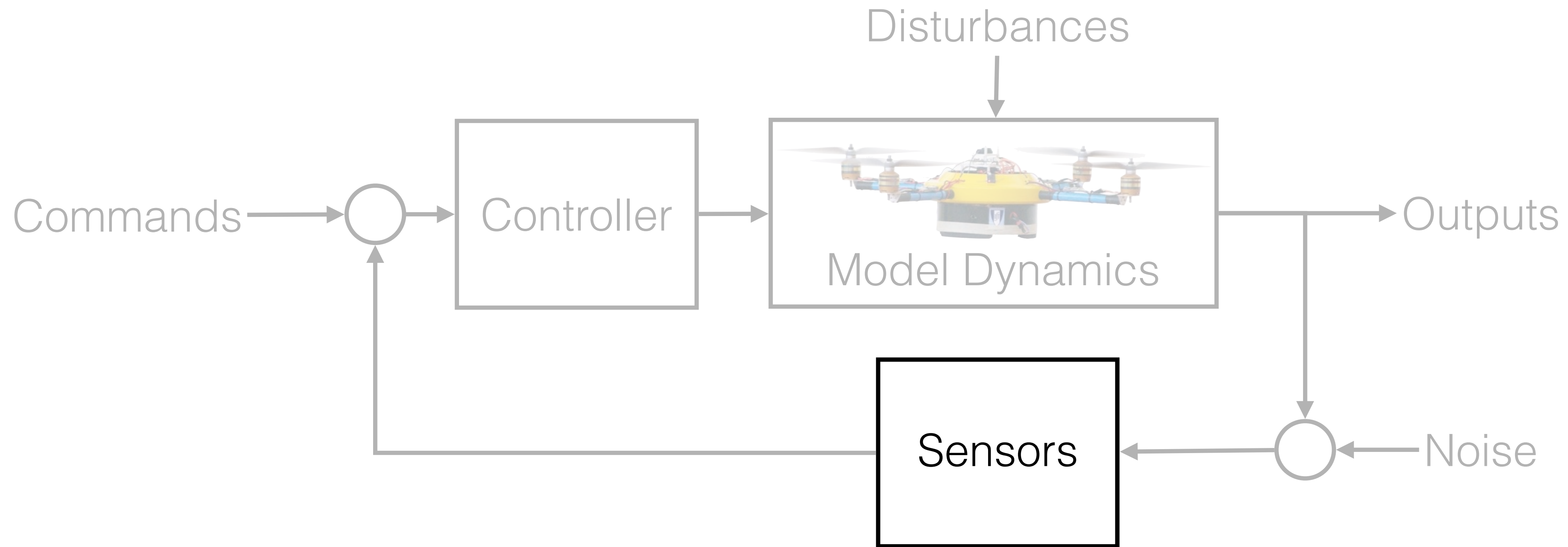
Trajectory Tracking Control



Desired position and yaw angle
 (p_d, ψ_d)



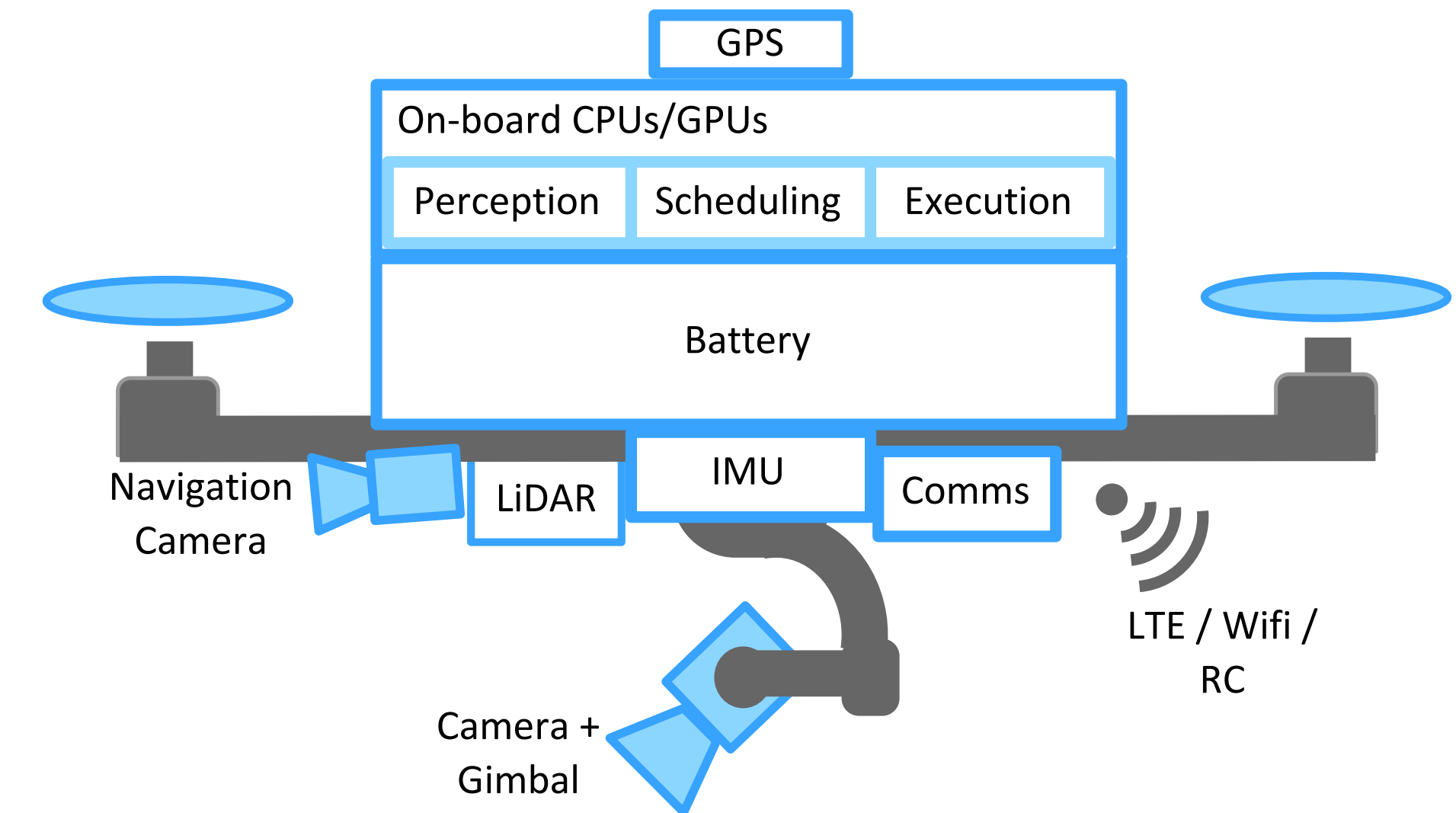
The quadrotor as a control system



Now the sensors

Sensors and Onboard Architecture

- Sensors
 - GPS - position estimates
 - IMU (accelerometers, gyroscopes, magnetometers) - attitude estimates
 - Cameras and LiDARs - mainly used for obstacle avoidance and task execution (surveying, inspection, ...)
- Onboard Computers
- Communication Systems
- Batteries



Biggest limitation to enhanced autonomy

- Flight time vs. available payload